

7. Hierarchies & Trees

Visualizing topological relations



Thorsten Buring, 06. Dezember 2007, Vorlesung Wintersemester 2007/08

Outline

≡ Hierarchical data and tree representations

≡ 2D Node-link diagrams

- ≡ Hyperbolic Tree Browser
- ≡ SpaceTree
- ≡ Cheops
- ≡ Degree of interest tree
- ≡ 3D Node-link diagrams

≡ Enclosure

- ≡ Treemap
- ≡ Ordered Treemaps
- ≡ Various examples
- ≡ Voronoi treemap
- ≡ 3D Treemaps

≡ Circular visualizations

≡ Space-filling node-link diagram

Hierarchical Data

- ≡ Card et al. 1999: data repository in which data cases are related to subcases
- ≡ Many data collections have an inherent hierarchical organization
 - ≡ Organizational Charts
 - ≡ Websites (approximately hierarchical)
 - ≡ File system
 - ≡ Family tree
 - ≡ OO programming
- ≡ Hierarchies are usually represented as tree visual structures
- ≡ Trees tend to be easier to lay out and interpret than networks (e.g. no cycles)
- ≡ But: as shown in the example, networks may in some cases be visualized as a tree

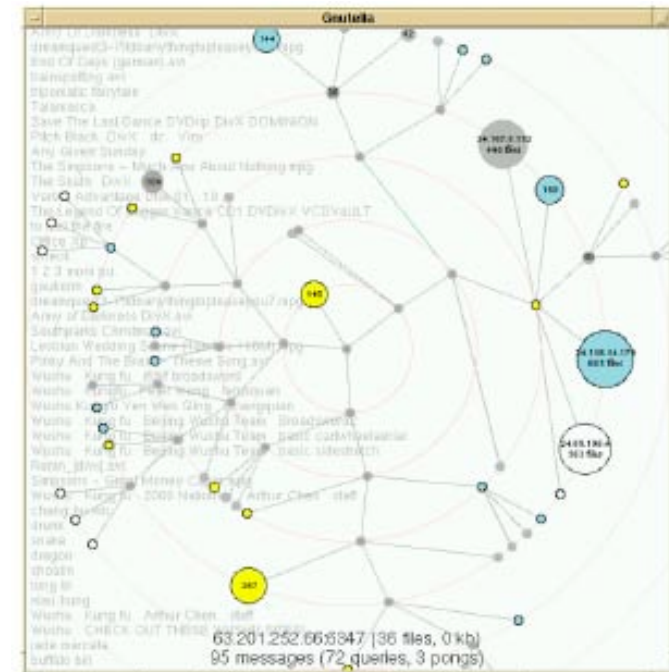


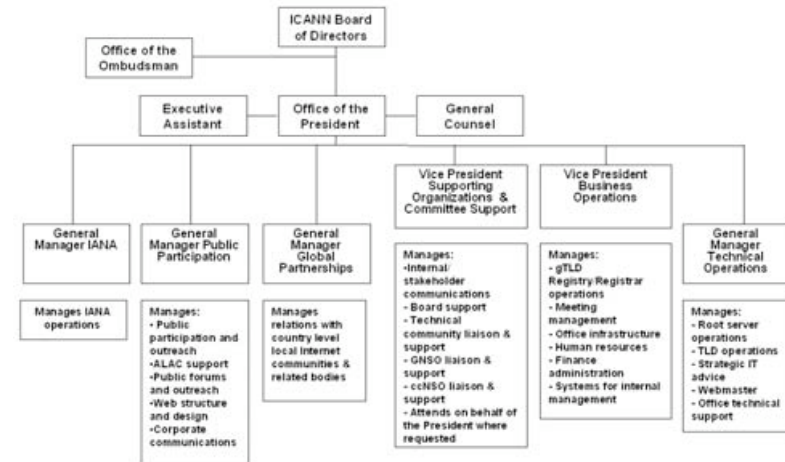
Figure 1: Visualization of the Gnutella network.

Yee et al. 2001

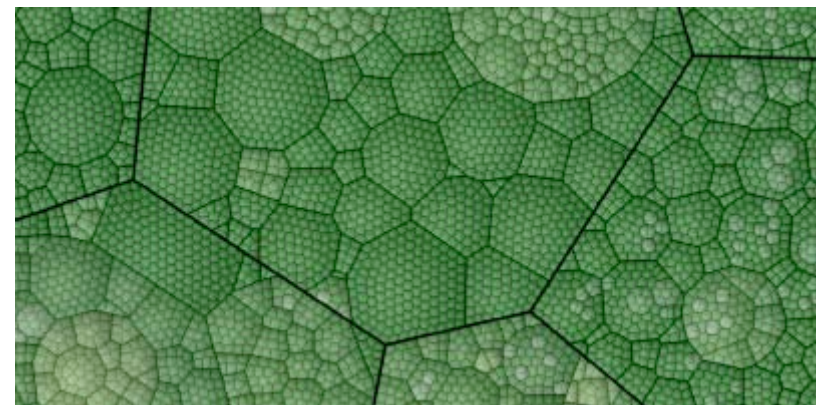
Tree Representations

- ≡ Two kinds of representations
- ≡ Node-link diagram (see previous lecture): represent connections as edges between vertices (data cases)
- ≡ Enclosure: space-filling approaches by visually nesting the hierarchy

ICANN ORGANIZATION CHART



<http://www.icann.org>



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- ≡ Enclosure

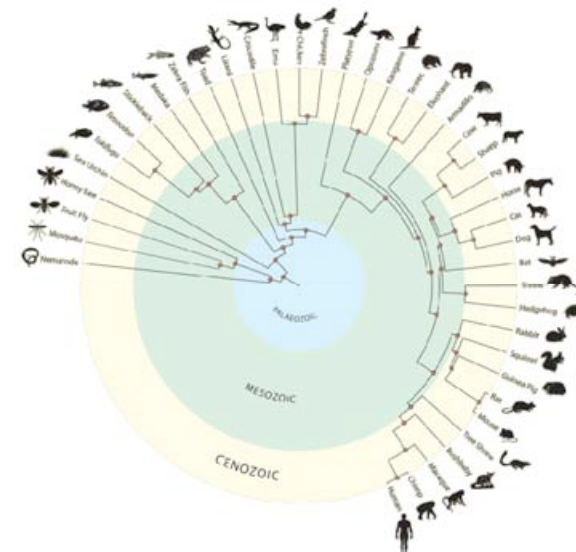
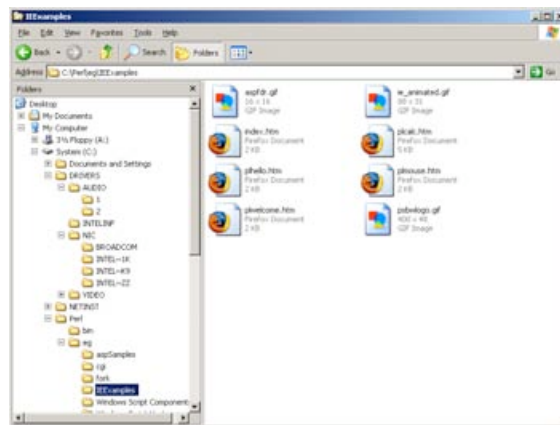
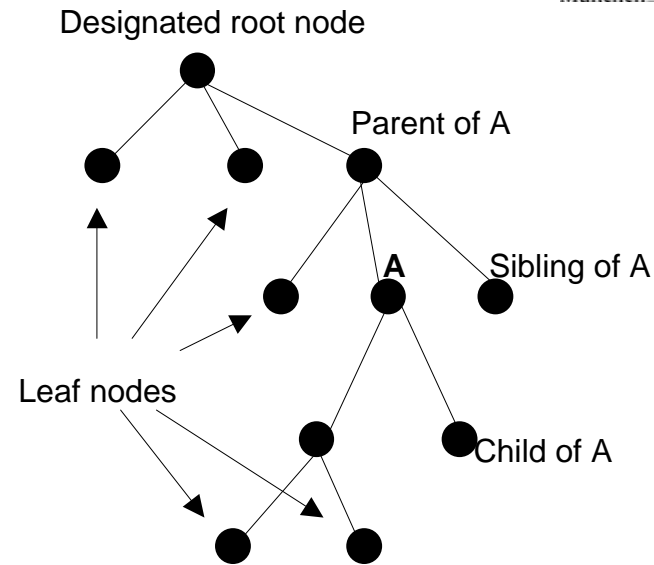
- ≡ Treemap
- ≡ Ordered Treemaps
- ≡ Various examples
- ≡ Voronoi treemap
- ≡ 3D Treemaps

- ≡ Circular visualizations

- ≡ Space-filling node-link diagram

Node-Link Diagram

- ≡ Most conventional layout
 - ≡ Tree-depth is mapped to an ordinal Y-axis
 - ≡ X-axis is nominal – mainly used to separate siblings
- ≡ Can also be turned around
- ≡ Circular layout – root in the center with levels growing outward



Node-Link Diagram

- ≡ Unlike space-filling methods node-link diagrams provide an effective overview of the topology of a tree
- ≡ Problems
- ≡ Large trees require an extreme aspect ratio
 - ≡ Example: branching factor of 2
 - ≡ Trees gets wider approximately proportionally 2^n ($n= \text{level}$)
 - ≡ Taller only proportionally to n
 - ≡ Large trees become to resemble a straight line
- ≡ Trees usually contain considerably empty space (about 50%)
- ≡ InfoVis approaches to address these problems
 - ≡ Interaction
 - ≡ Distortion



Image from: <http://davenation.com/doitree/doitree-avi-2002.htm>

Hyperbolic Tree Browser

- ≡ Lamping et al. 1995
- ≡ Comparable to fisheye distortion
 - ≡ Nodes in the center are displayed at higher granularity
 - ≡ Neighboring nodes are displayed in diminishing size
- ≡ Maximum number of nodes displayed in a 600 x 600 pixel window
 - ≡ Standard 2D hierarchy browser: typically 100 nodes with 3 characters text labels
 - ≡ Hyperbolic browser: can display 1000 nodes with 50 nearest the focus can show from 3 to dozens of characters text labels
- ≡ Approach exploits hyperbolic geometry
 - ≡ Lay out hierarchy on hyperbolic plane and map plane onto a circular display region
 - ≡ Property of hyperbolic plane: circumference of a circle grows exponentially with its radius
 - ≡ Hierarchies tend to expand exponentially with depth
 - ≡ Elegant match!

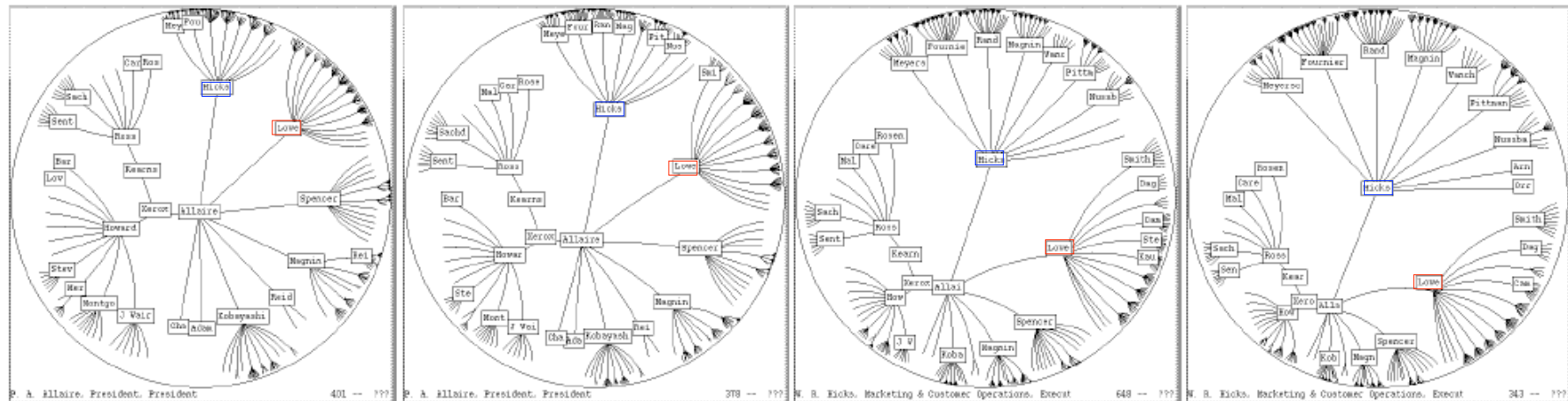


Inspiration:
Circle Limit IV by M.C. Escher

Hyperbolic Tree Browser

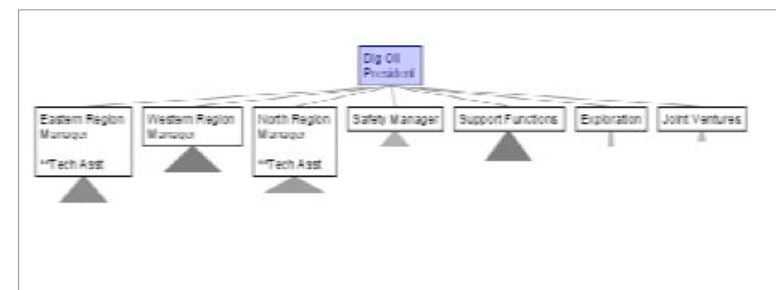
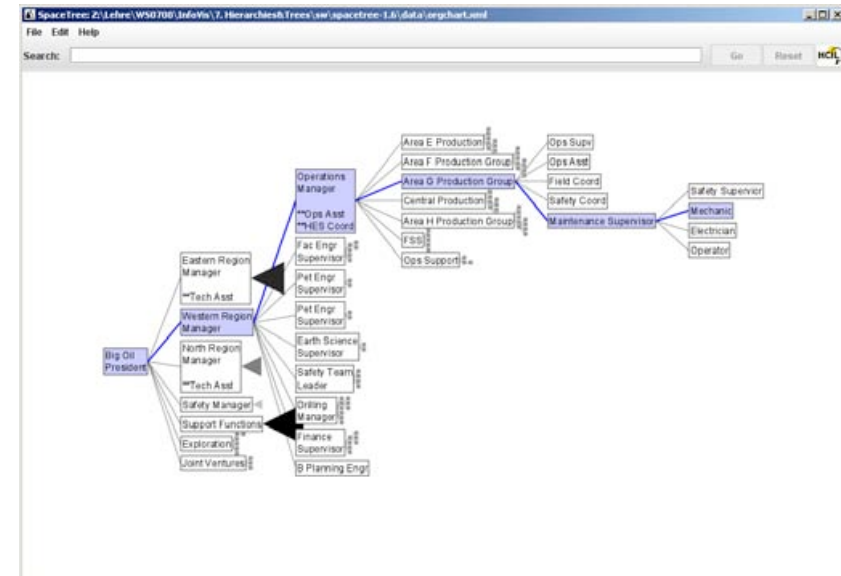
- ≡ Navigation: users select nodes to become the new center node (animated transitions)
- ≡ Potential problem with orientation:
 - ≡ nodes rotate during pure translation, e.g. node “Lowe” moves from top right to bottom right
 - ≡ Not suitable to present data such as organizational charts
- ≡ Small-scale user test (4 subjects, within-subjects design, IV: type of browser, DV: number of actions, time, preference)
 - ≡ No significant performance advantage over a 2D hierarchy browser with horizontal tree layout
 - ≡ Participants preferred the hyperbolic tree browser - provided “weaker sense of directionality of links”, but helped to “get(ting) a sense of the overall tree structure”
- ≡ <http://www.inxight.com/products/sdks/st/index.php> - **Demo**

Lamping et al. 1995



SpaceTree

- ≡ Plaisant et al. 2002
- ≡ Mechanisms to facilitate large tree exploration / navigation
 - ≡ Dynamic rescaling of branches to fit the screen
 - ≡ De-composed animated transitions
 - ≡ Optimized camera movement
 - ≡ Preview icons summarizing branches collapsed (see top-down order)
 - ≡ Shading of triangle is proportional to the total number of nodes in the subtree
 - ≡ Height of triangle represents depth of subtree
 - ≡ Base of triangle proportional to average width (number of items / depth)
 - ≡ Search and filter functionality
- ≡ Demo

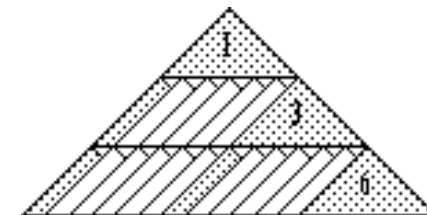
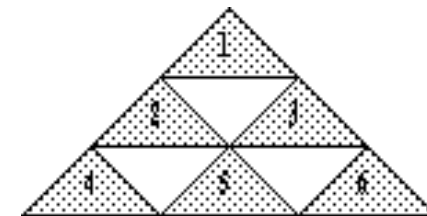
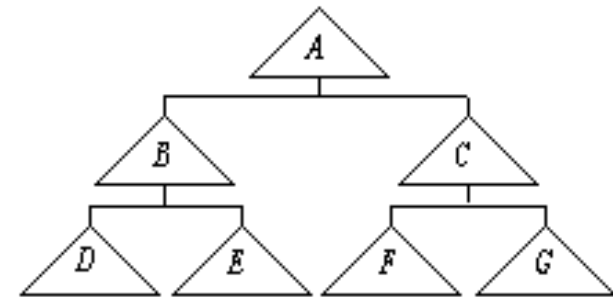


SpaceTree

- ☰ Experiment comparing 3 tree-browsing interfaces
 - ☰ Microsoft Explorer
 - ☰ Hyperbolic tree browser
 - ☰ SpaceTree
- ☰ Counterbalanced repeated-measures within-subject design
- ☰ 18 participants
- ☰ Tree with 7000 nodes
- ☰ Three task types
 - ☰ Node searches
 - ☰ Search of previously visited nodes
 - ☰ Answering topology questions
- ☰ Results
 - ☰ Hardly significant performance differences between the interfaces
 - ☰ Users found MS Explorer significantly less attractive than the other two interfaces

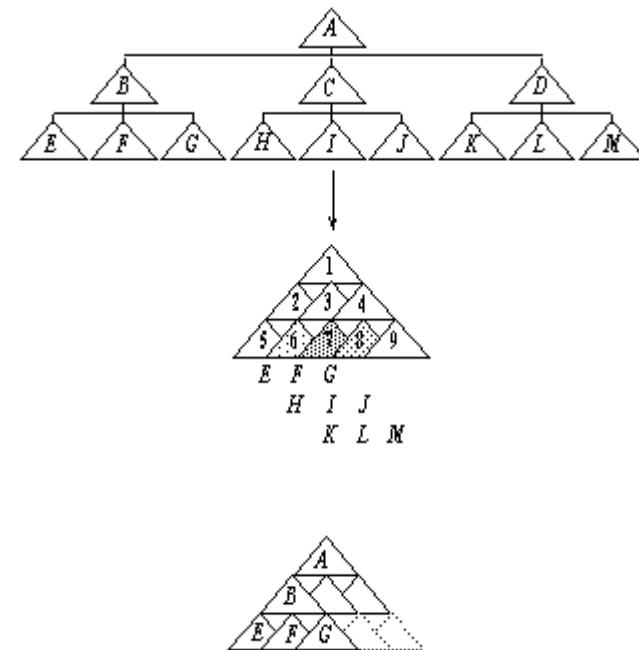
Cheops

- ≡ Beaudoin et al. 1996
- ≡ Exploring and navigating large graphs
 - ≡ Maintain context
 - ≡ Provide easy access to details
- ≡ Cheops provides effective compression by reusing visual components based on interaction
- ≡ Compress the hierarchy by tessellation of triangles
 - ≡ In the example triangle 5 could represent either node E or node F
 - ≡ If triangle 2 is selected, triangle 5 will become node E ...
 - ≡ Overlapping triangles to indicate larger hierarchy
 - ≡ The example shows an expansion by adding 5 children per parent
- ≡ But: users cannot compare topologically remote parts of a structure



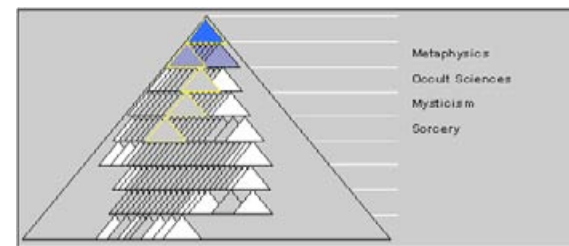
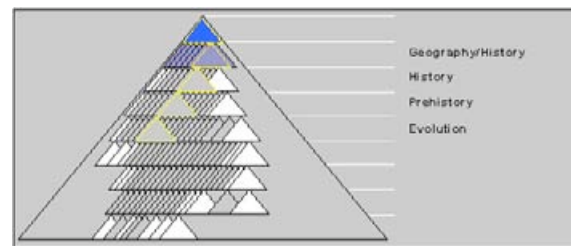
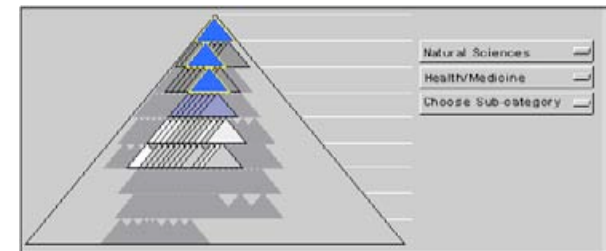
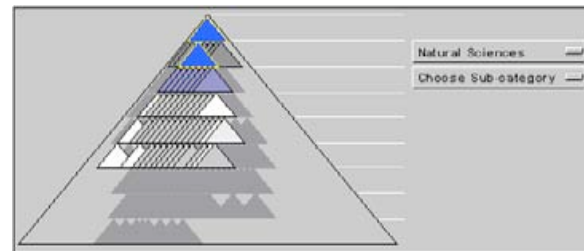
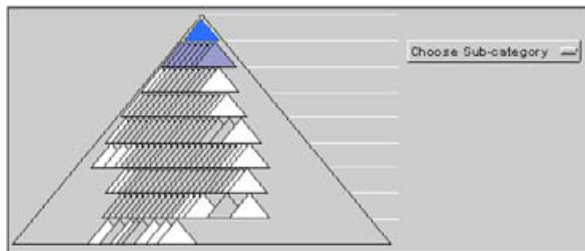
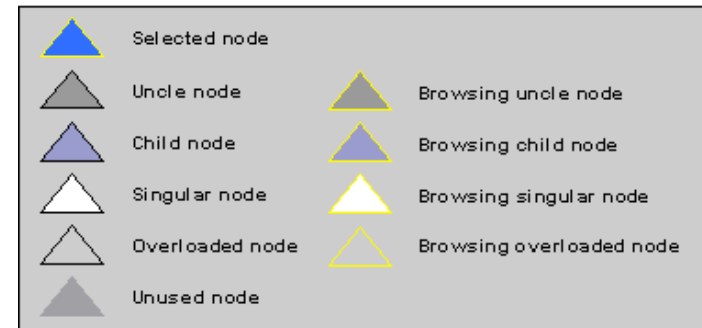
Cheops

- ≡ Another example
- ≡ Three triangles in the last level represent more than one logical node
- ≡ If a parent node (e.g. B) is selected the visual components become unambiguous
- ≡ Selection of a node implies previous selection of all its parent nodes
- ≡ Nodes are represented as paths of visual objects going down from the root – not isolated triangles



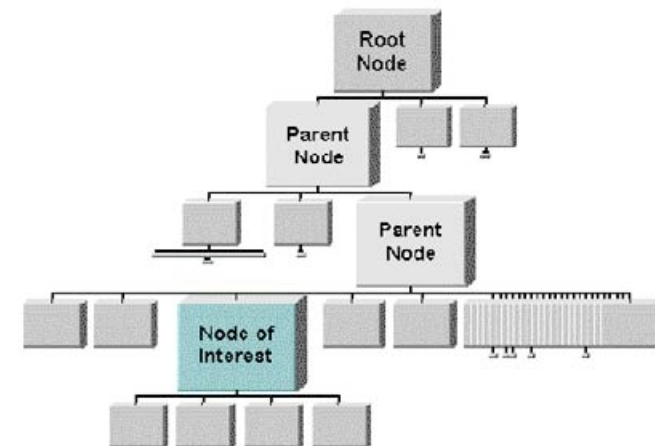
Cheops

- ≡ Visual cues and terminology to aid interpretation of the compressed visualization
- ≡ Selection: deployment of branches
- ≡ Pre-selection: direct access to any node in the tree



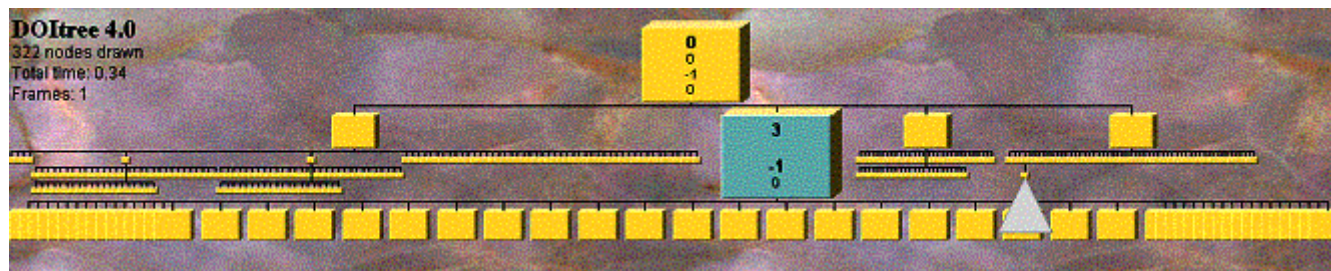
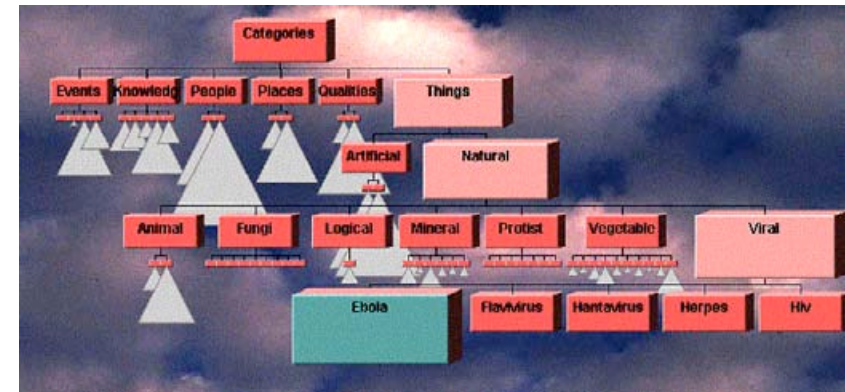
Degree of Interest Tree

- ≡ Nation et al. 2002
- ≡ For interactive display of hierarchies within a web browser
- ≡ Based on Furnas Degree-of-interest function
 - ≡ Each node is assigned a value
 - ≡ Degree-of-interest value is determined by a function of a node's distance from the root of the tree and its distance from the focus of interest
 - ≡ Topic of later lecture on focus+context presentation techniques!
- ≡ DOITree
 - ≡ Upon selection: focused node is allocated most space
 - ≡ Remaining space is allocated to nodes based on their DOI values
 - ≡ Nodes with more space present more details



Degree of Interest Tree

- ≡ Animated transitions
- ≡ Reset the tree layout by clicking on the root node
- ≡ Tree does not fit the screen in the Y-dimension
 - ≡ Prune parts of the tree below a given DOI threshold
 - ≡ Pruned branch is represented by a symbol
- ≡ Tree does not fit the screen in the X-dimension – visually compress peripheral nodes



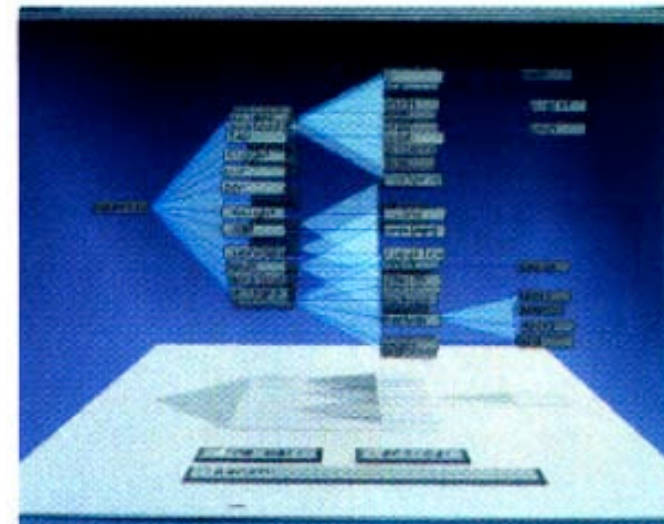
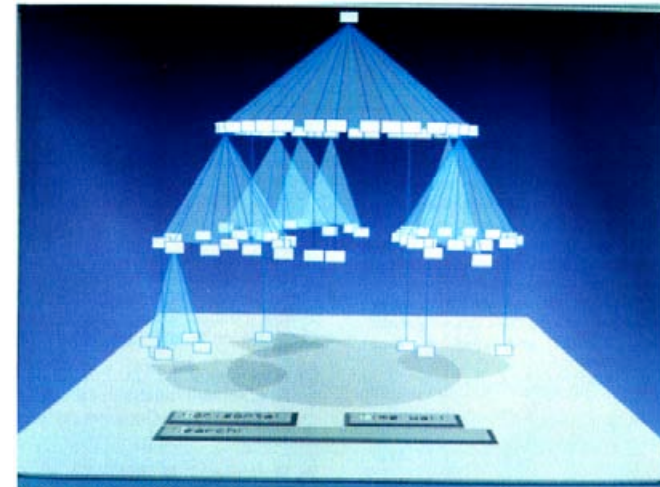
Images from: <http://davenation.com/doitree/doitree-avi-2002.htm>

3D Approaches

- ≡ Why not use an additional dimension to visualize nodes that would otherwise be pruned / collapsed?
 - ≡ Cone Tree
 - ≡ H3Viewer
- ≡ HCI research produced mixed results about the usability of 3D interfaces
- ≡ Ongoing research question: do 2D interfaces better exploit the abilities of the human perceptual system?
 - ≡ Utilize spatial memory?
 - ≡ Controlling 3D navigation with 2D input devices?
- ≡ 3D node-link approaches have been mainly researched in the 90s

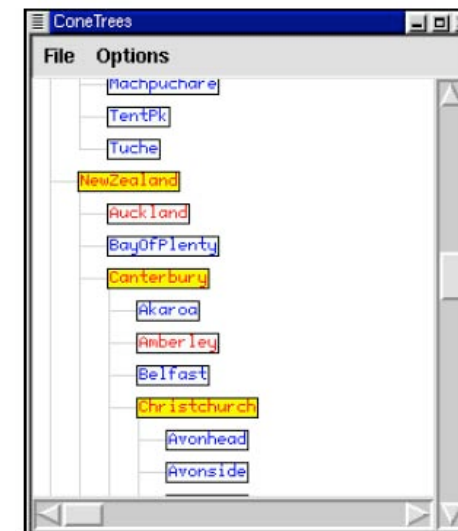
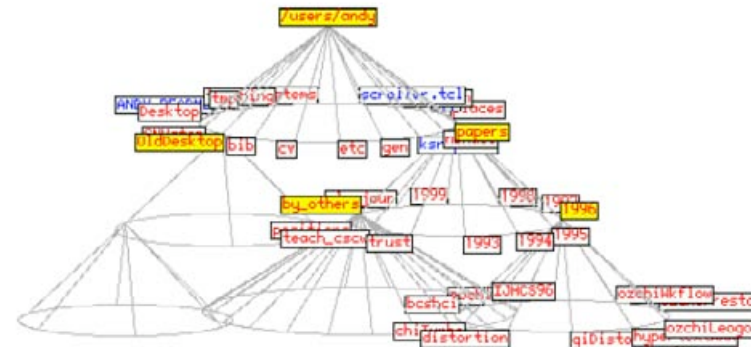
Cone Tree

- ≡ Robertson et al. 1991
- ≡ Use depth to make more effective use of screen space
- ≡ Hierarchies laid out uniformly in three dimensions
- ≡ When a node is selected by a user the tree rotates to bring the node to the front
- ≡ Animation to make the users comprehend the rotation
- ≡ Problem: still clutter and occlusion
- ≡ Movie



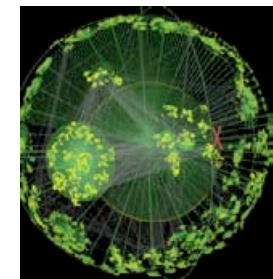
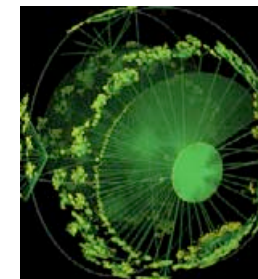
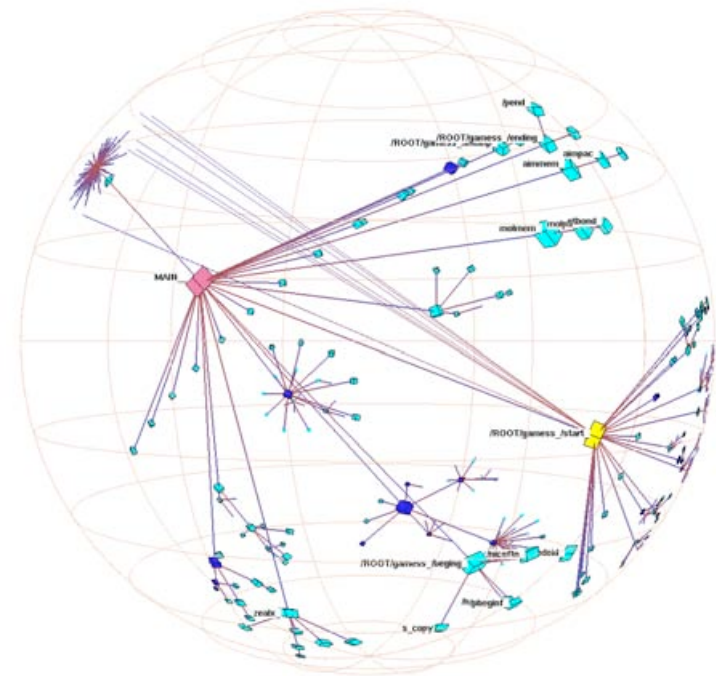
Cone Tree

- ≡ Usability evaluation by Cockburn & McKenzie 2000
- ≡ Compare Cone Tree to conventional explorer-like 2D tree browser
- ≡ User test with 12 participants
- ≡ Independent variables: depth, density of tree, interface type
- ≡ Dependent variables: task-completion time, user preference
- ≡ Results
 - ≡ Users were slower in locating data using the Cone Tree
 - ≡ Performance deteriorated rapidly with a growing branching factor
 - ≡ But: participants clearly preferred the Cone Tree...



H3Viewer

- ≡ Munzner 1997
- ≡ H3Viewer supports interactive exploration of large graphs (> 100,000 edges)
- ≡ Graph is presented in 3D hyperbolic space
- ≡ Child nodes are distributed on the surface of a hemisphere
- ≡ Users can drag and rotate graph
- ≡ Demo
- ≡ Java 3D implementation and gallery:
<http://www.caida.org/tools/visualization/walrus/>



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☰ Degree of interest tree

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☰ Enclosure

☰ Treemap

☰ Ordered Treemaps

☰ Various examples

☰ Voronoi treemap

☰ 3D Treemaps

☰ Circular visualizations

☰ Space-filling node-link diagram

Treemap

≡ Johnson & Shneiderman 1992

≡ Basic idea

- ≡ Map hierarchical data to rectangular 2D display area by recursively partitioning the screen into rectangular boxes representing nodes
- ≡ Utilize 100% of the screen

≡ Less good for analyzing the topology of a tree

≡ Advantages

- ≡ Very effective when focusing on leaf nodes and their attributes
- ≡ More suitable for additional encoding via color, size, shape
- ≡ Present large hierarchies on a single screen

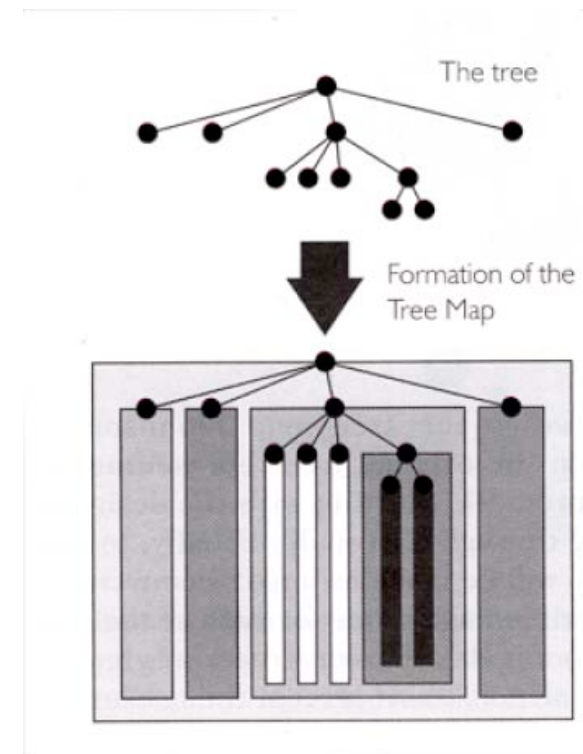
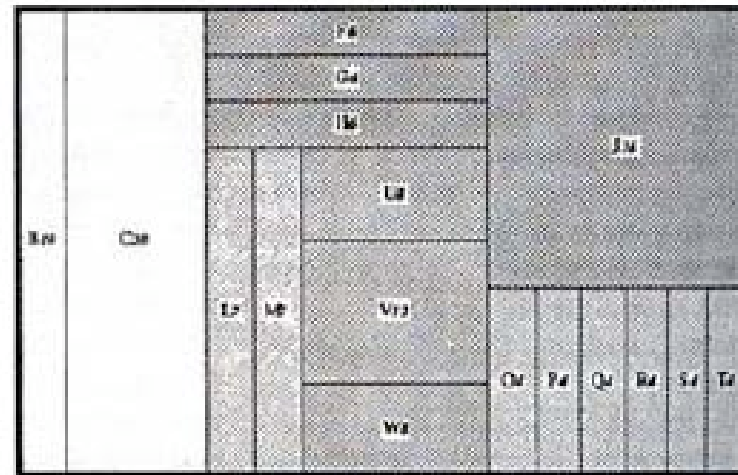
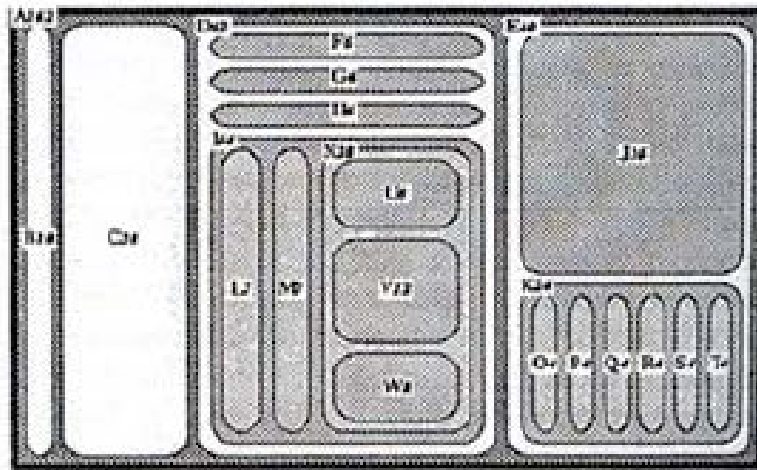


Image taken from Spence 2007

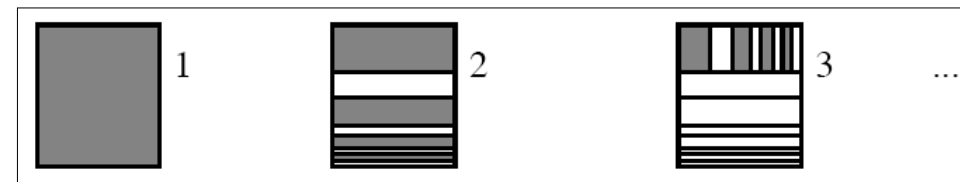
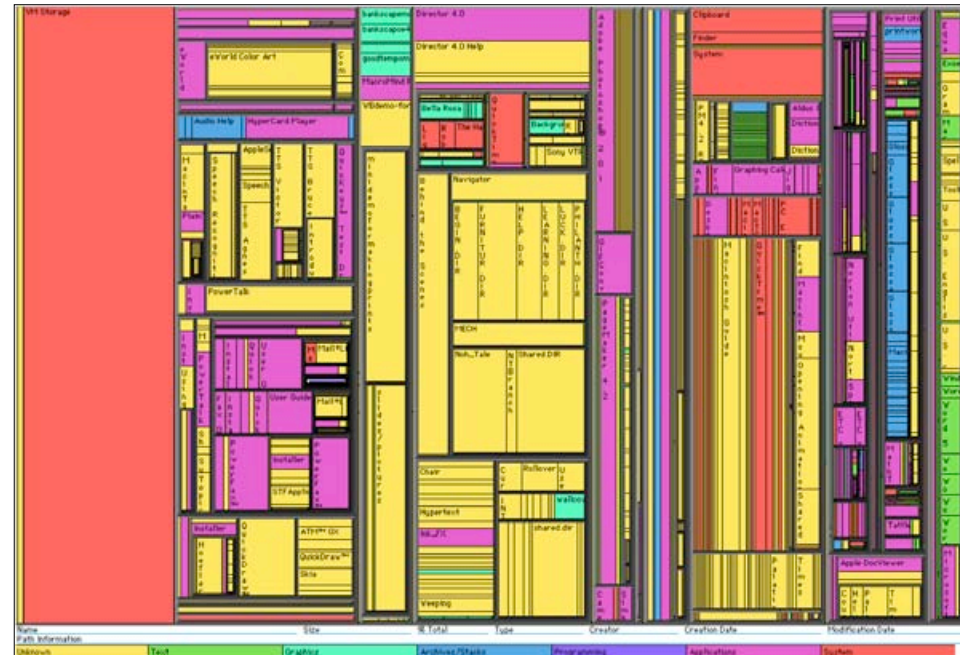
Treemap

≡ Nested versus non-nested Treemaps



Treemap

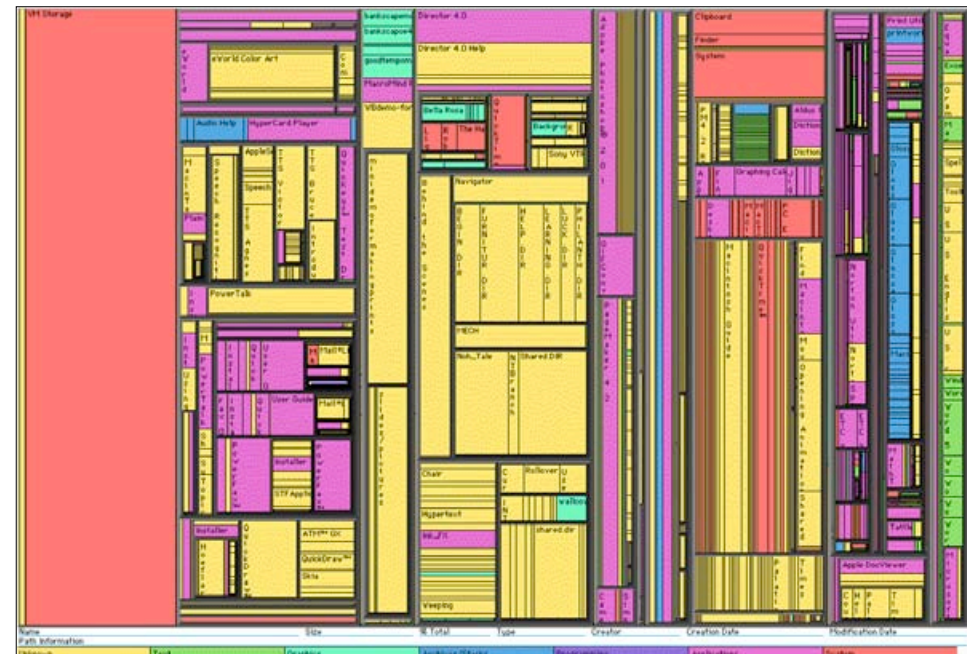
- ≡ Shneiderman 1992
- ≡ Slice and dice algorithm
 - ≡ Use parallel lines to divide a rectangle representing an item into smaller rectangles representing the item's children
 - ≡ Each child is allocated a size proportional to some property (additional encoding by color)
 - ≡ At each level of the hierarchy switch the orientation of the lines (vertical vs. horizontal)
- ≡ Example application: file browser
 - ≡ Size: file size, color: file type
 - ≡ Users can easily identify large file
 - ≡ Detect duplicate directories
 - ≡ ...



<http://ftpdim.uqac.ca/pub/ychirico/wvdr2002/nigay.pdf>

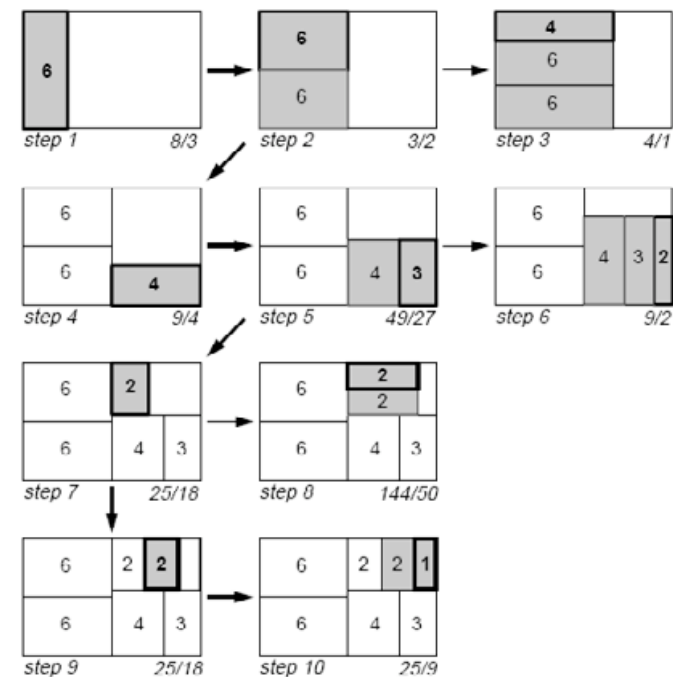
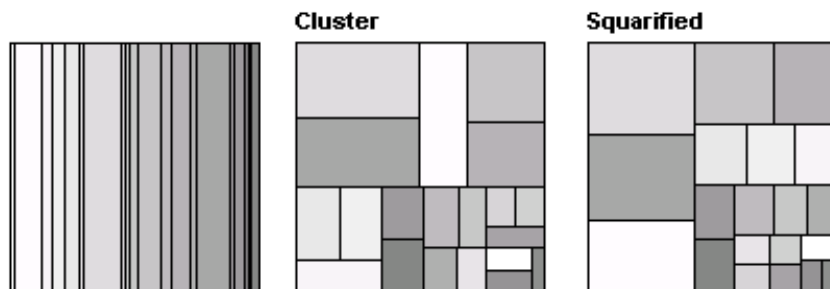
Treemap

- ≡ Problems with this layout?
- ≡ Creates layouts that contain many rectangles with a high aspect ratio
- ≡ Thin rectangles are hard to see, select, label and compare in size
- ≡ Which of the blue rectangles is bigger?



Treemap

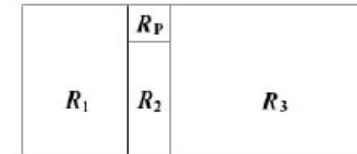
- ≡ Several algorithms to create more useful tree-maps by reducing the overall aspect ratios of the map rectangles
- ≡ Cluster algorithm (Wattenberg1999): employ both vertical and horizontal partitions at each level of the hierarchy
- ≡ Squarification algorithm (Bruls et al. 2000)
- ≡ Sorts and adds the input rectangles ordered by size
- ≡ Problem of both algorithms
 - ≡ Changes in the data set can cause dramatic layout changes (hard to track items given dynamic data)
 - ≡ Given ordering of items is not preserved (as indicated by shading)



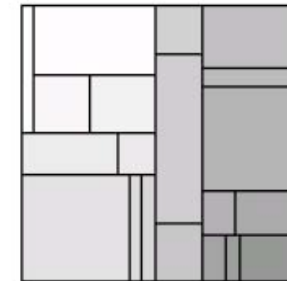
Subdivision algorithm for squarified algorithm (Bruls et al. 2000)

Ordered Treemap

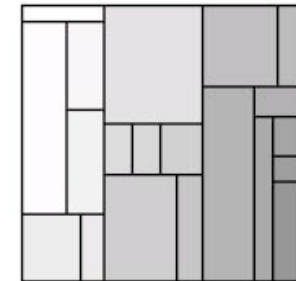
- ≡ Seek compromise between smooth updates and low aspect ratios
- ≡ Items are given as a list ordered by index and have varied areas
- ≡ Items that are next to each other in the given order should be approximately adjacent in the tree-map
- ≡ Shneiderman & Wattenberg 2001
- ≡ Pivot-by-size & Pivot-by-middle
 - ≡ Partition area into 4 regions
 - ≡ Pick pivot element R_p
 - ≡ Size: largest item
 - ≡ Middle: middle item
 - ≡ Depending on the aspect ratio of R , place R_p in horizontal oder vertical middle
 - ≡ R_1 : items earlier in the list than pivot (sublist L_1)
 - ≡ R_2 : items in list before R_3 such that their overall size makes R_p have aspect ratio closest to 1 (sublists L_2 , and L_3)
 - ≡ Apply steps recursively for areas R_1 , R_2 , and R_3



Pivot-by-middle

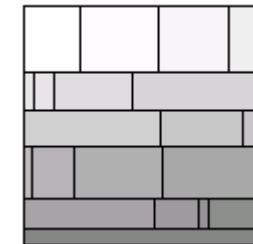
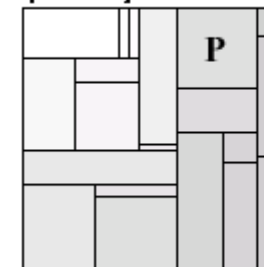
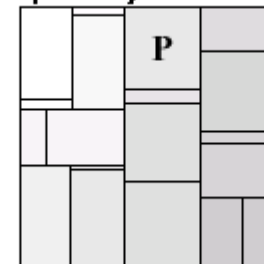


Pivot-by-size



Ordered Treemap

- Strip treemap - Bederson & Shneiderman 2002
- Modification of squarified algorithm
- Produces better readability than basic ordered treemap algorithms and comparable aspect ratios (only slightly worse than unordered squarified algorithm)
- Rectangle is filled stepwise with strips
- Strip is filled stepwise with rectangles as long as the average aspect ratio of the strip decreases or stays the same
- Otherwise a new strip is added

StripTreemap**pivot-by-size****pivot-by-middle**

Ordered Treemap

- ≡ Test with several generated data sets
- ≡ Table shows results for three levels of hierarchy and eight items at each level
- ≡ 100 trials of 100 steps each
- ≡ Comparing the algorithms by **average aspect ratio** and **average layout distance change** (how much do rectangles move as data is updated) and **readability** (how easy it is to visually scan a layout to find a particular item)
- ≡ Tradeoff between low aspect ratios and smooth updates!

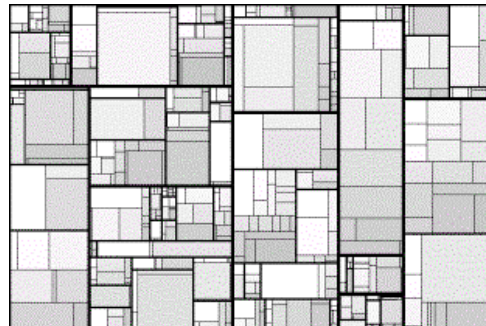
Algorithm	Aspect Ratio	Change	Readability
Slice-and-dice	26.10	0.46	1.0
Pivot-by-middle	3.58	1.21	0.42
Pivot-by-size	3.31	4.14	0.33
Pivot-by-split	3.00	2.37	0.35
Strip	2.83	1.09	0.51
Cluster	1.79	7.67	0.26
Squarified	1.74	8.27	0.26

Ordered Treemap

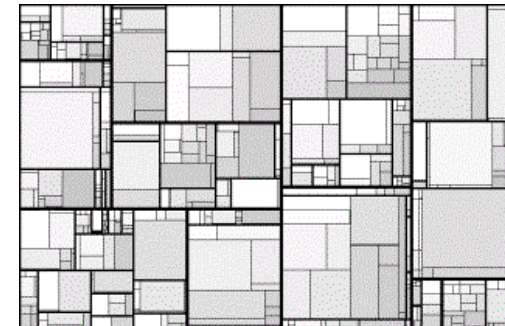
- ≡ Applying the algorithms to real-world data - confirmed prior test results
- ≡ Set of 535 publicly traded companies, market capitalization as the size attribute
- ≡ Gray scale indicates ordering within each industry group that is the last level of hierarchy in this data set



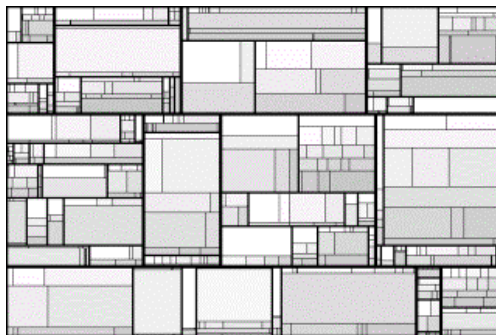
Slice-and-dice layout



Pivot-by-middle layout.

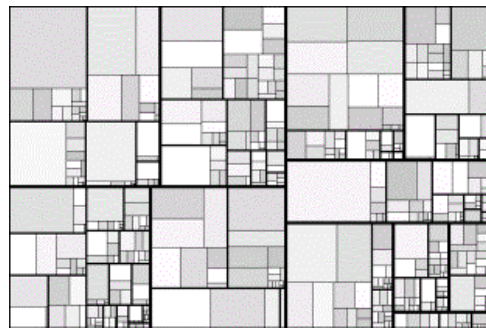


Pivot-by-size layout



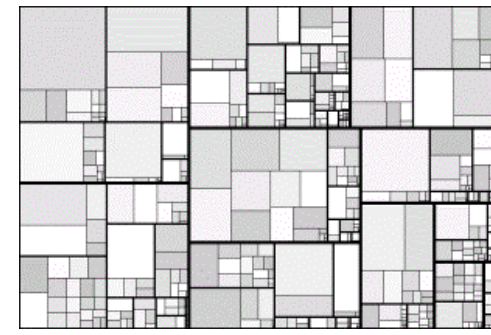
Strip layout

LMU Department of Media Informatics



Cluster layout

www.medien.ifi.lmu.de



Squarified layout.

thorsten.buring@ifi.lmu.de

Ordered Treemap

☰ Compare algorithms

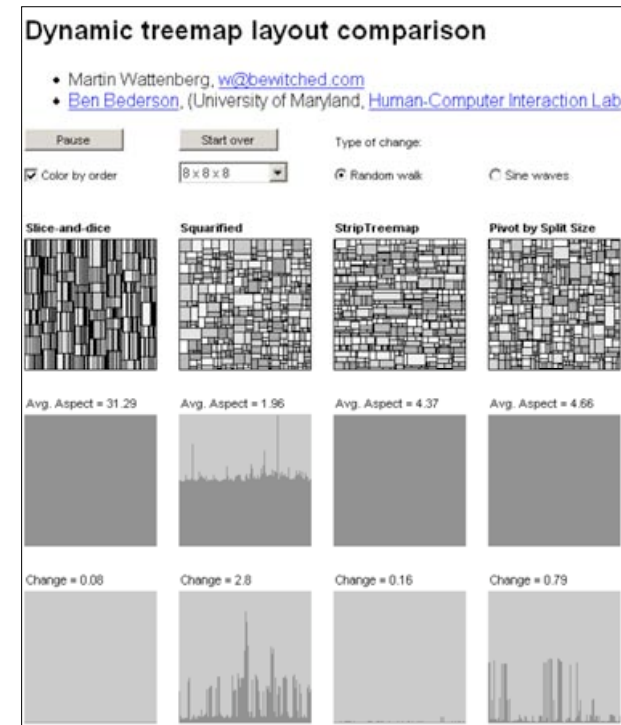
http://www.cs.umd.edu/hcil/treemap-history/java_algorithms/LayoutApplet.html

☰ History of treemaps

<http://www.cs.umd.edu/hcil/treemap-history/>

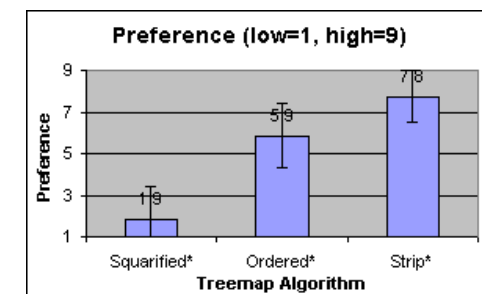
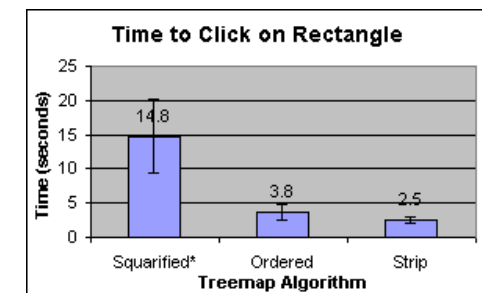
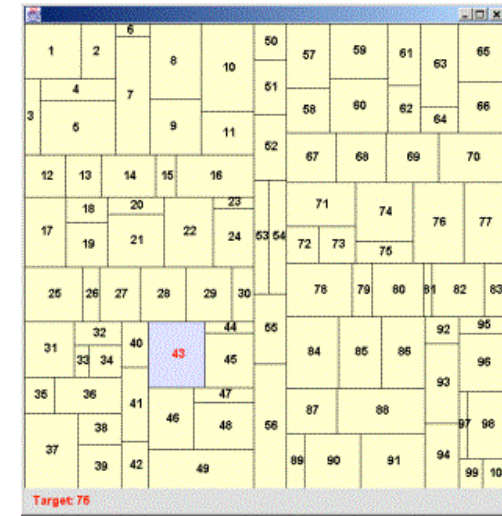
☰ Java 1.1 library for five Tree-map algorithms:

<http://www.cs.umd.edu/hcil/treemap-history/Treemaps-Java-Algorithms.zip>



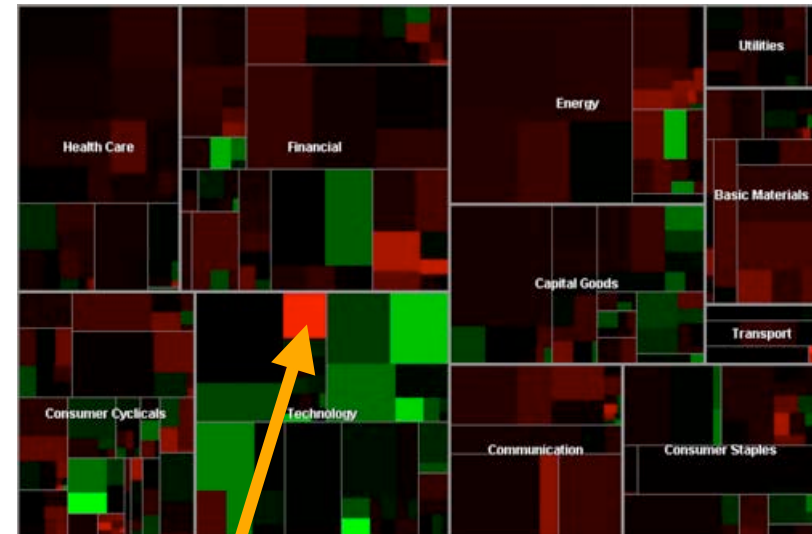
Ordered Treemap

- ≡ Bederson et al. 2002
- ≡ User study of layout readability
- ≡ Compared the squarified, pivot-based, and strip treemap algorithms
- ≡ 20 Participants had to identify a specific rectangle by clicking on the rectangle with the requested numerical ID
- ≡ Repeated-measures design
- ≡ Independent variable: treemap algorithm
- ≡ Dependent variable: time, subjective user rating
- ≡ Time: significant difference between squarified algorithm and the other two
- ≡ Preference: significant difference between all three algorithms
- ≡ Validates readability metric used



Map of the Market

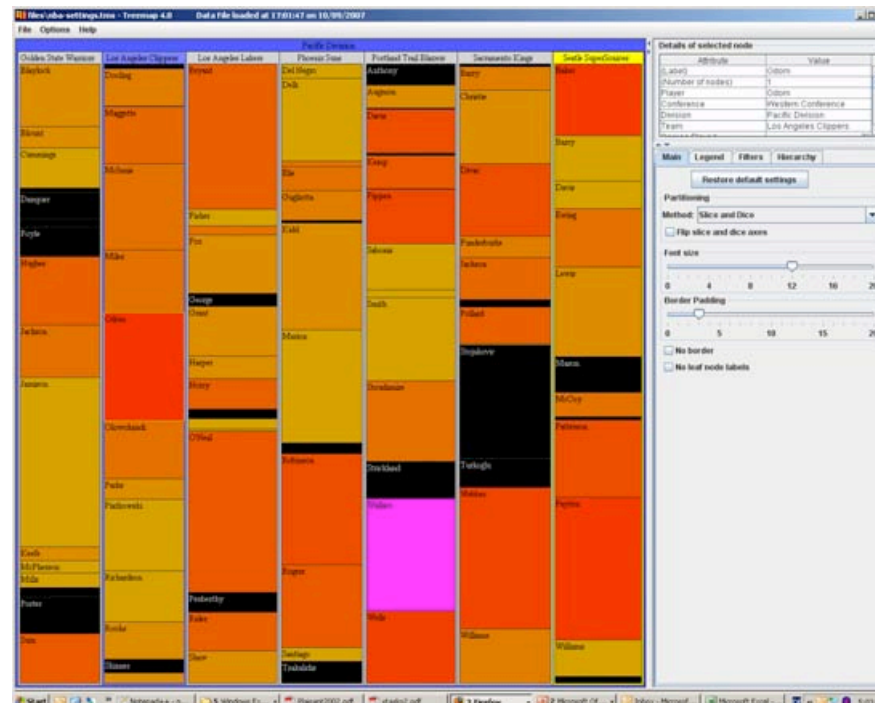
- ≡ Wattenberg 1999
- ≡ Cluster treemap to reduce overall aspect ratios
- ≡ <http://www.smartmoney.com/marketmap/>
- ≡ 500 stocks updated every 15 minutes
- ≡ Each rectangle represents a company
 - ≡ Size: company's market capitalization
 - ≡ Color: price performance
- ≡ Double-ended multiple hue color coding
 - ≡ Green: stock price is up
 - ≡ Red: stock price is down
 - ≡ Black: neutral, no change
- ≡ Detailed information on-demand
- ≡ Demo



SAP Pays \$6.8 Billion for Business Objects

Treemap 4.1

- ☰ Human-Computer Interaction Lab – University of Maryland
- ☰ Applet: <http://www.cs.umd.edu/hcil/treemap/index.shtml>
- ☰ Demo



Some Treemaps Online

NewsMap



Peet's Coffee: Coffee Selector

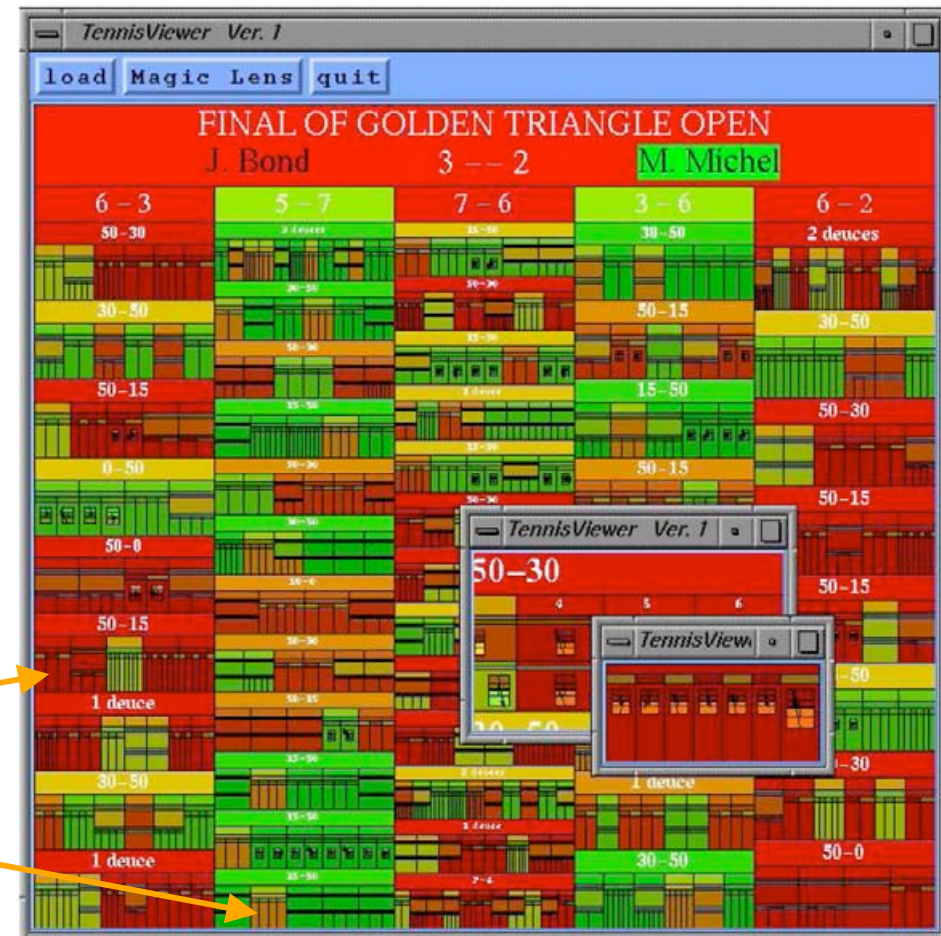


iTunes Top 100



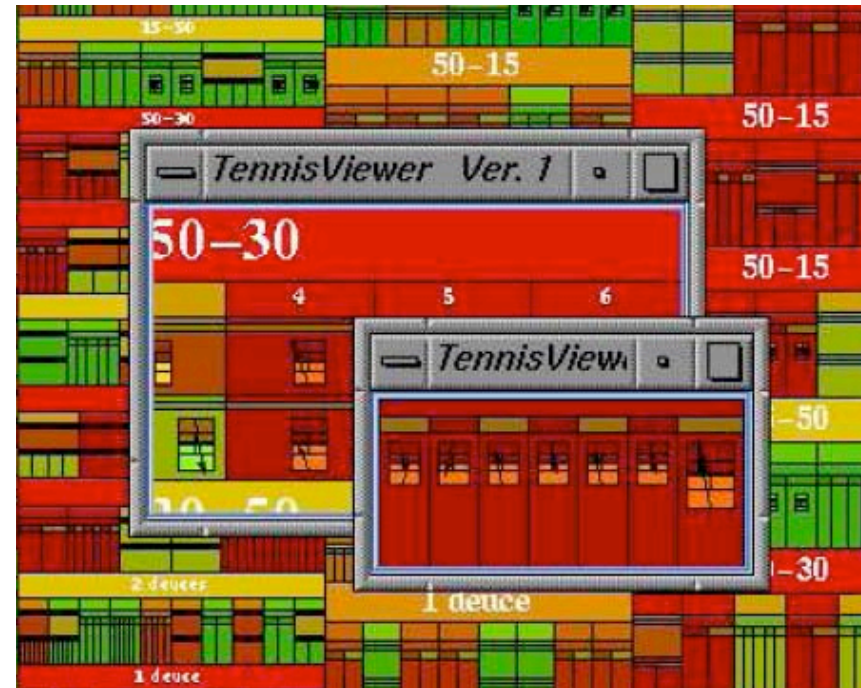
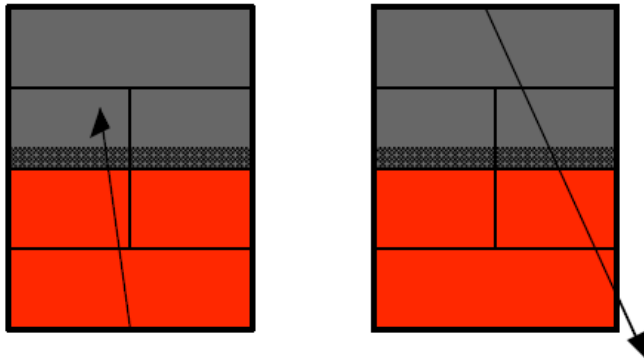
TennisViewer

- ≡ Jin & Banks 1997
- ≡ Visualize a tennis match using a treemap
- ≡ Match tree
 - ≡ Root node – the tennis match
 - ≡ Match node subdivides horizontally into sets
 - ≡ A set subdivides vertically into games
 - ≡ A game subdivides horizontally into points
- ≡ Color mapping of rectangles show node ownership (who won what?)
- ≡ Translucent child rectangles are layered over parent rectangles
 - ≡ Point of a winning effort
 - ≡ Point of a losing effort



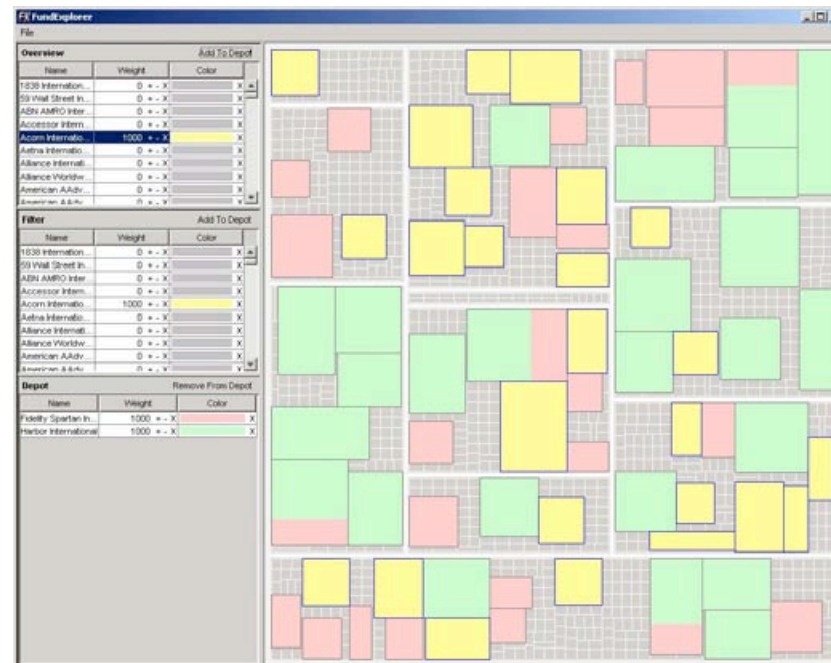
TennisViewer

- ☰ Magic Lens to explore ball traces
- ☰ Example: the return of a service goes out of bounds



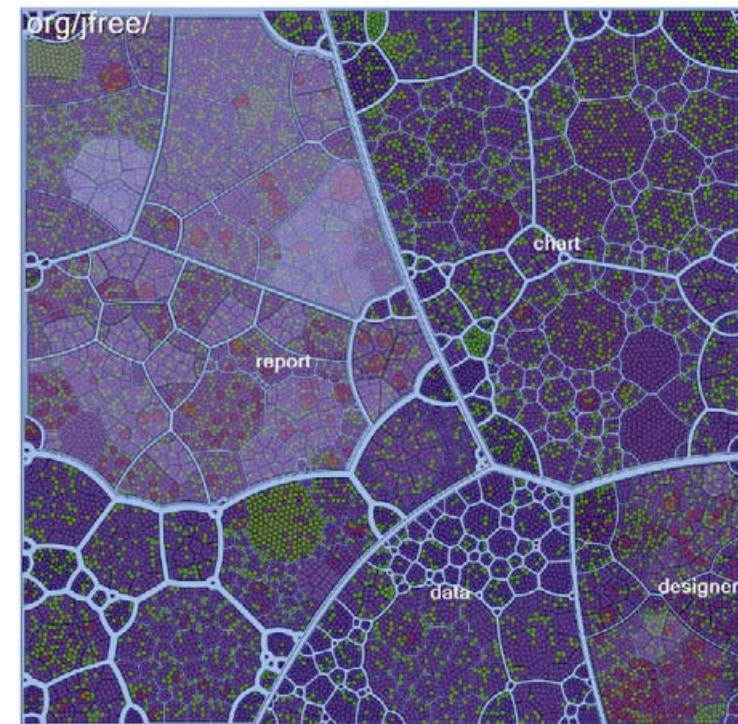
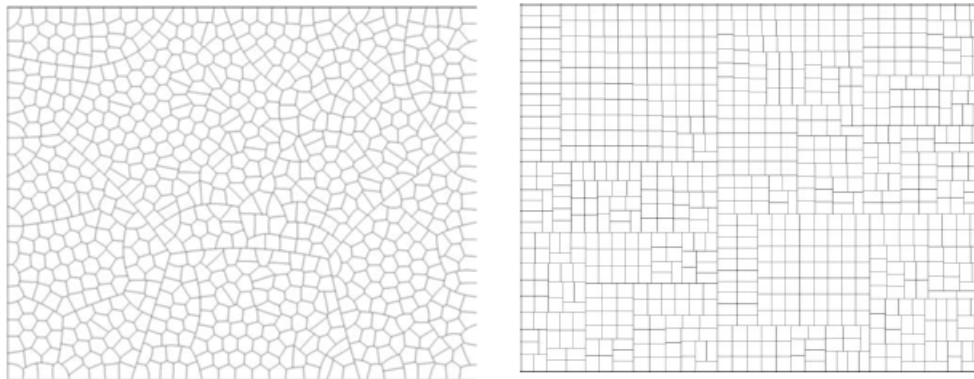
FundExplorer

- ≡ Csallner et al. 2003
- ≡ To support the diversification of mutual fund portfolios, i.e. how to find funds with little overlap in their investments
- ≡ Also show stocks with zero investment
- ≡ Movie



Voronoi Treemap

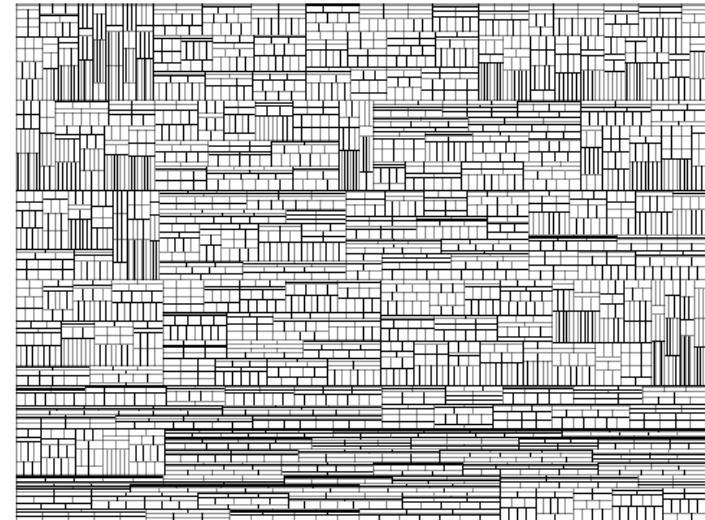
- ≡ Balzer et al. 2005
- ≡ Treemap consisting of arbitrary polygons instead of rectangles
 - ≡ Aspect ratio of polygons converges to 1
 - ≡ Polygons are distinguishable due to the irregular shapes
 - ≡ Avoid that edges of different objects run into each other



Cushion Treemap

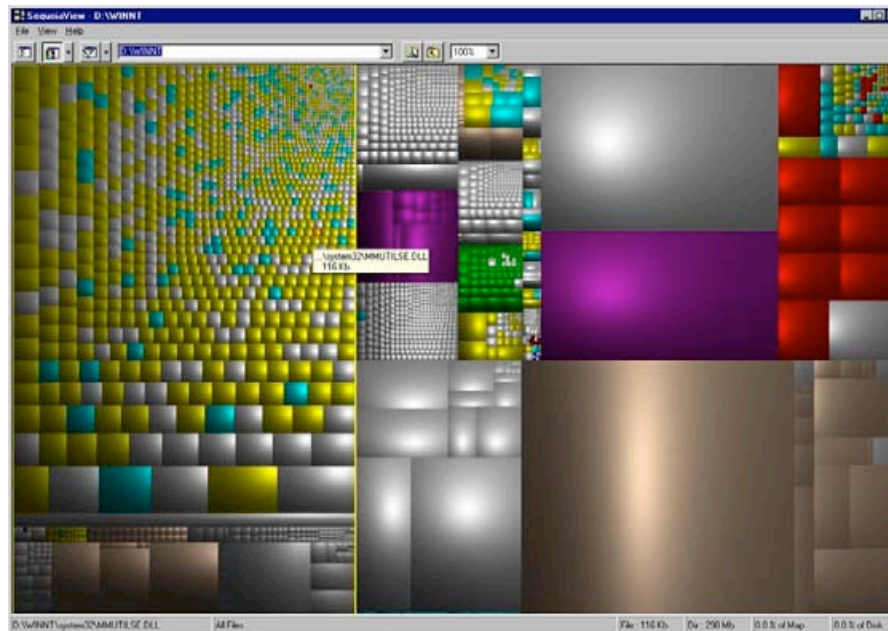
- ≡ Wijk & van de Wetering 1999
- ≡ Treemaps usually fall short to visualize the structure of the tree
- ≡ Worst case: a balanced tree, where each parent has the same number of children and each leaf has the same size
- ≡ Outcome: regular grid
- ≡ Nested treemap may reduce this problem, but:
 - ≡ Margins require screen space
 - ≡ Deeply nested trees are difficult to read
- ≡ Idea: add shading and texture to help convey the structure of the tree

Cushion Treemap



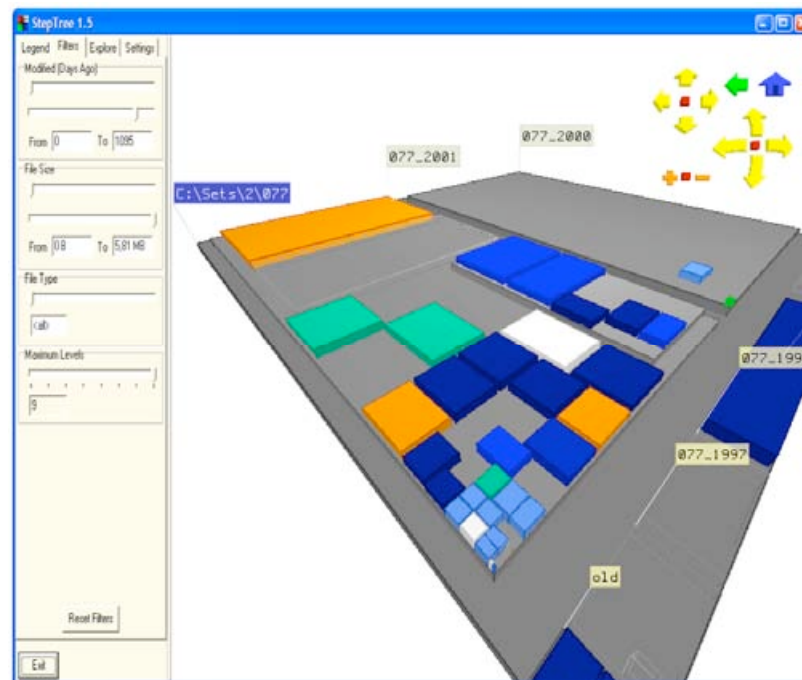
Cushion Treemap

- ≡ SequoiaView
- ≡ http://w3.win.tue.nl/nl/onderzoek/onderzoek_informatica/visualization/sequoiaview//
- ≡ Visualizes the contents of your hard drive



StepTree

- ≡ Bladh et al. 2004
- ≡ Convey tree structure via third dimension
- ≡ <http://www.sm.luth.se/csee/csn/visualization/filesysvis.php>

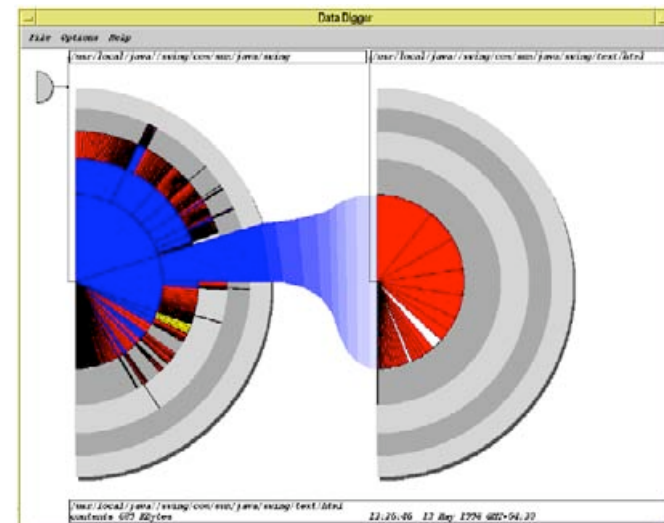
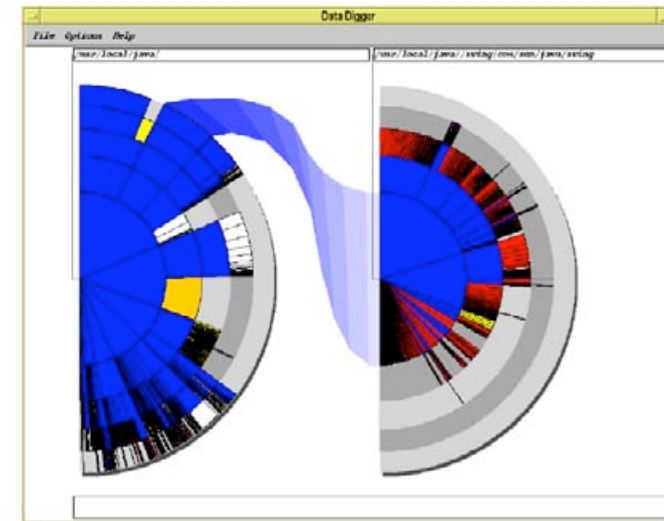


Outline

- ☰ Hierarchical data and tree representations
- ☰ 2D Node-link diagrams
 - ☰ Hyperbolic Tree Browser
 - ☰ SpaceTree
 - ☰ Cheops
 - ☰ Degree of interest tree
 - ☰ 3D Node-link diagrams
- ☰ Enclosure
 - ☰ Treemap
 - ☰ Ordered Treemaps
 - ☰ Various examples
 - ☰ Voronoi treemap
 - ☰ 3D Treemaps
- ☰ Circular visualizations
- ☰ Space-filling node-link diagram

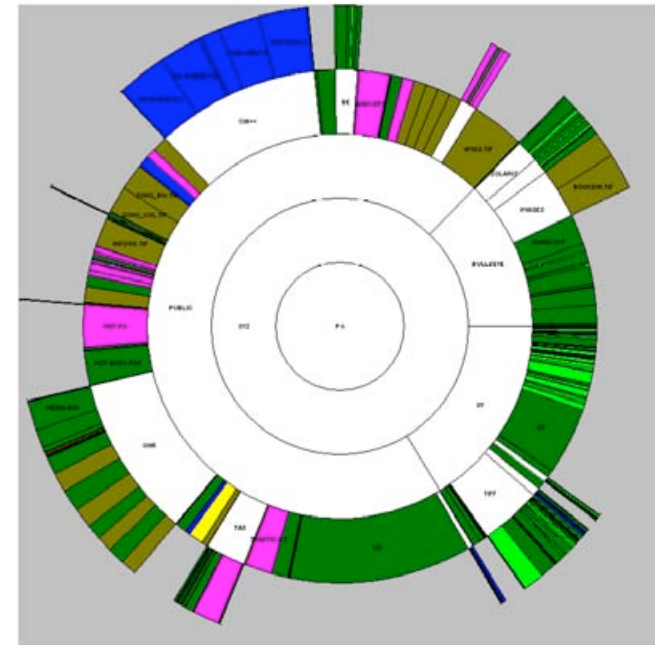
Information Slices

- ≡ Andrews & Heidegger 1998
- ≡ Visualization is based on one or more semi-circular discs
- ≡ Each disc represents multiple levels (5 to 10, configurable) of a hierarchy
- ≡ Files and directories deeper in the hierarchy are drawn further from the center
- ≡ Child nodes are drawn within the arc subtended by their parents
- ≡ For deeper hierarchies multiple discs are cascaded
- ≡ Example shows Solaris JDK, 6158 files in 502 directories, maximum depth of 9 levels
- ≡ Blue: directories, other colors: file type



Sunburst

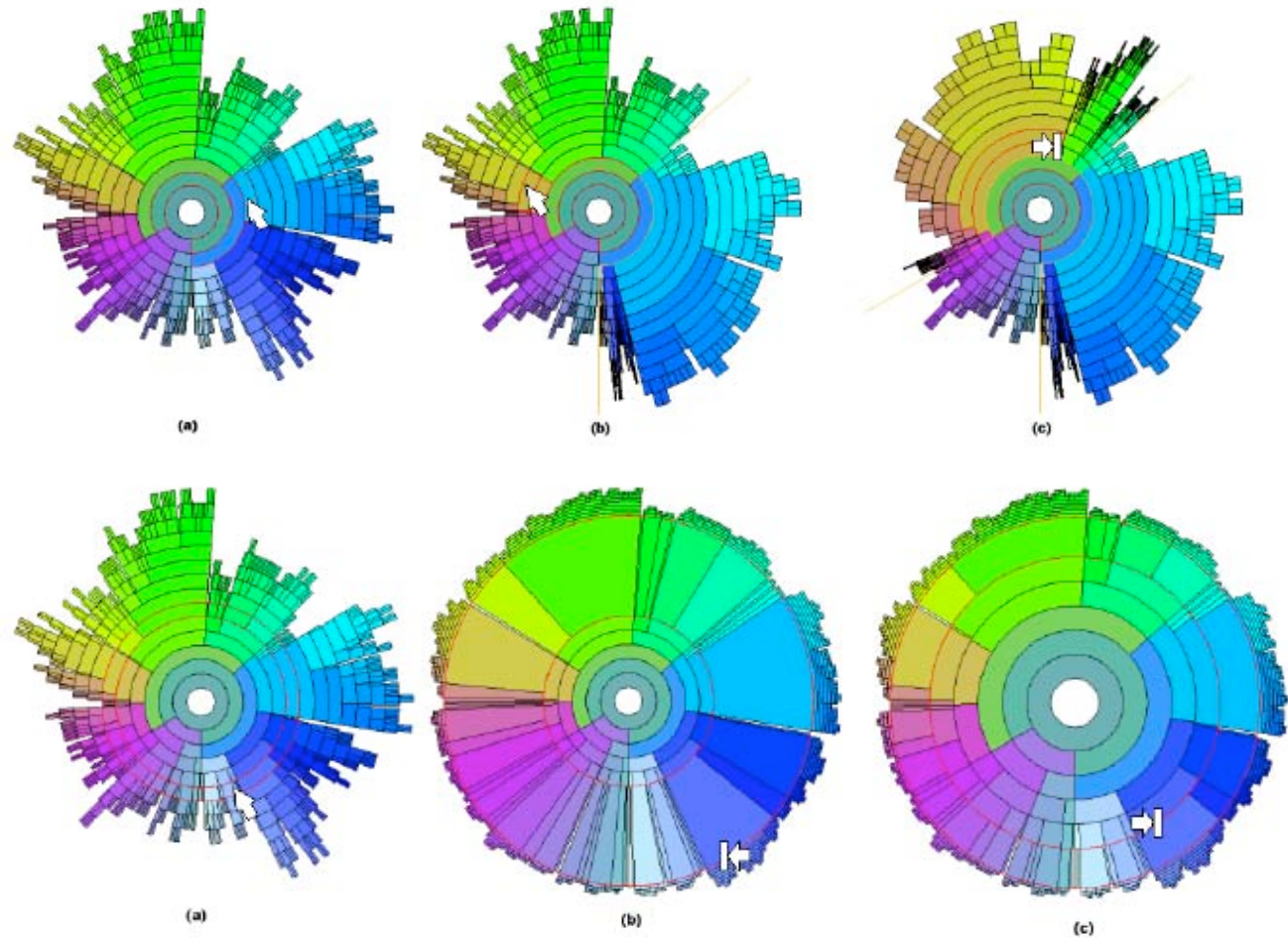
- ≡ Stasko & Zhang 2000
- ≡ Full circular visualization to give each element more space
- ≡ Navigating the tree should not lead to significant node position changes (e.g. hyperbolic browser)
- ≡ Three animated approaches to provide a focus area while maintaining context
 - ≡ Angular detail method
 - ≡ Detail outside method
 - ≡ Detail inside method
- ≡ Comparative evaluation of sunburst vs. treemap did not show significant differences in task completion times, but participants strongly preferred sunburst (Stasko et al. 2000)
- ≡ Radial visualizations may better depict the structure of the tree, but are not as space-efficient as treemaps
- ≡ **Movie**



Sunburst visualizing file structure

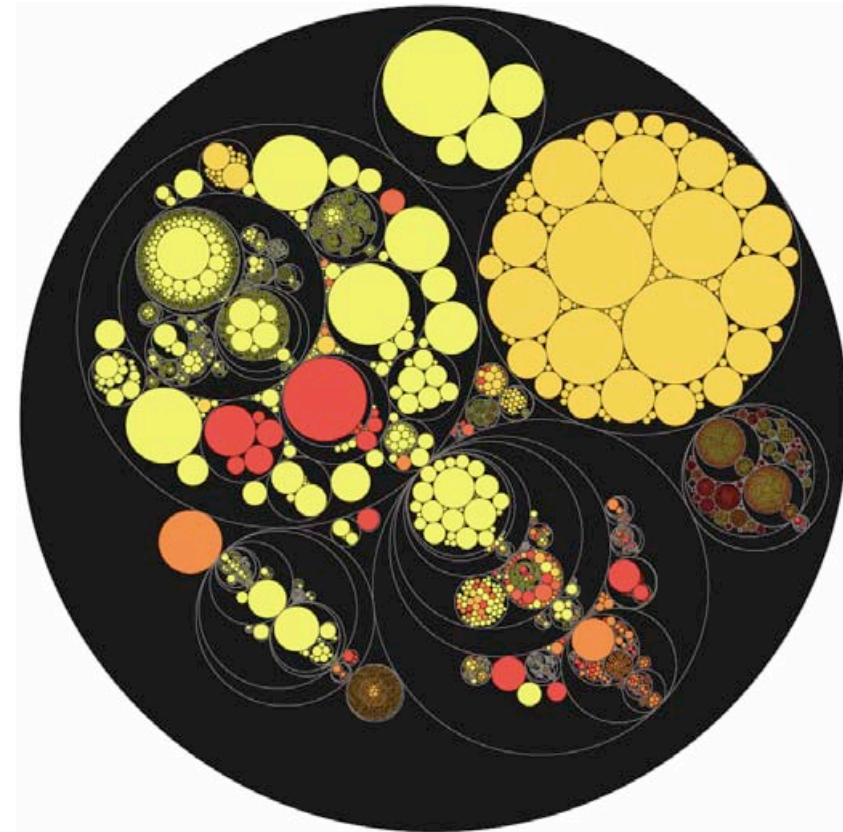
Interring

- ≡ Yang et al. 2002
- ≡ Multiple foci (circular distortion + radial distortion)



Circular Treemaps

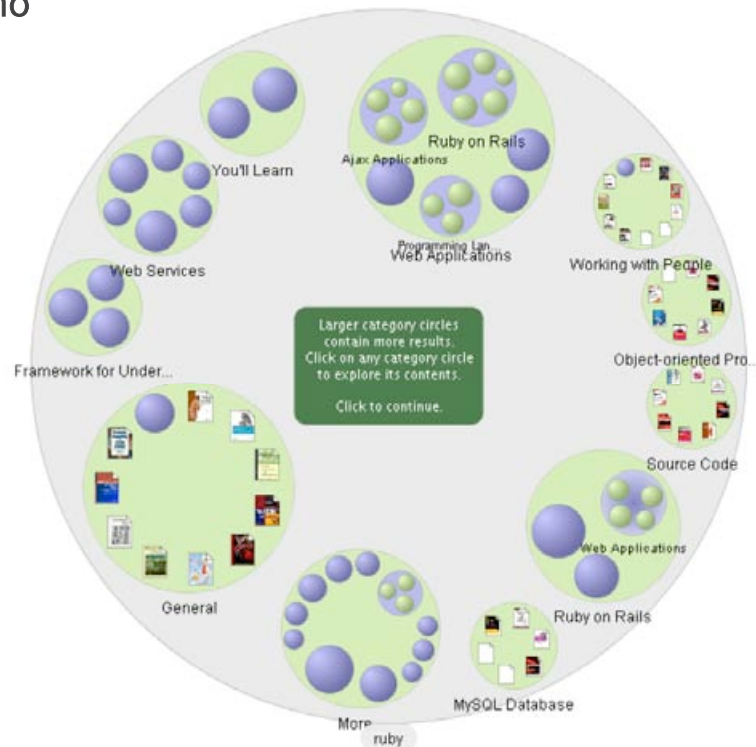
- ≡ Kay Wetzel
- ≡ Do not fill space completely
- ≡ But
 - ≡ Aspect ratio stays the same for all elements
– easy comparison of sizes
 - ≡ Good visibility of nesting (though at the cost of unused space)
 - ≡ Rather beautiful layout!



Visualization of a file system with color mapping for creation data

Circular Treemaps

- ☰ Grokker - <http://live.grokker.com/>
- ☰ Clustering search results as nested circles
- ☰ Demo

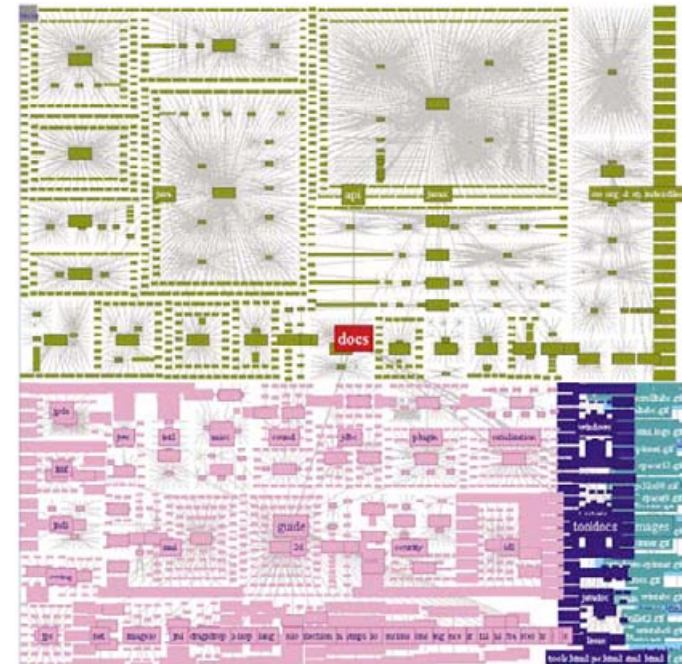


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 - ≡ 3D Treemaps
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- ≡ Space-filling node-link diagram

Enclosure + Connection

- ≡ EncCON: Nguyen & Huang 2005
- ≡ Connection (node-link)
 - ≡ Gives immediate perception of data relationships and the tree structure
 - ≡ Not efficient regarding display space utilization: most pixels are wasted as background
- ≡ Enclosure (e.g. treemaps)
 - ≡ Space-filling approach allows the display large trees on a single glance
 - ≡ Focus on the leaf nodes but hardly conveys the tree structure
- ≡ Idea: combine **enclosure** and **connection** approach
- ≡ Child nodes are not embedded but placed around parent nodes using a circular, space-filling division method
- ≡ Focus+context navigation



Java SDK visualization – 9500 directories and files

Obligatory Literature

- ≡ N. Henry, J.-D. Fekete, and M. J. McGuffin: "NodeTrix: A Hybrid Visualization of Social Networks", 2007.
- ≡ Benjamin B. Bederson & Ben Shneiderman , "Ordered and Quantum Treemaps: Making Effective Use of 2D Space to Display Hierarchies", 2002.